

# A Scalable AMR Gravity Solver for ENZO-E (Extreme-scale ENZO)

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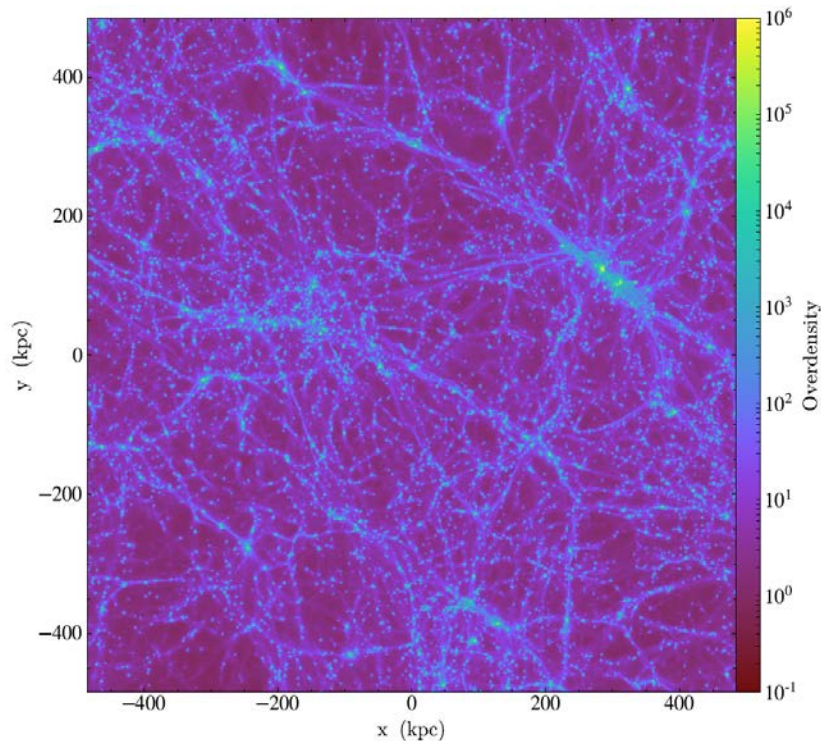
University of California, San Diego

*Supported by NSF grants CSSI-1835402, SI2-SSE-1440709, PHY-1104819,  
PRAC-1516003, PRAC-1810774*

# Science Motivation: Large-scale simulations of the IGM including galaxy feedback

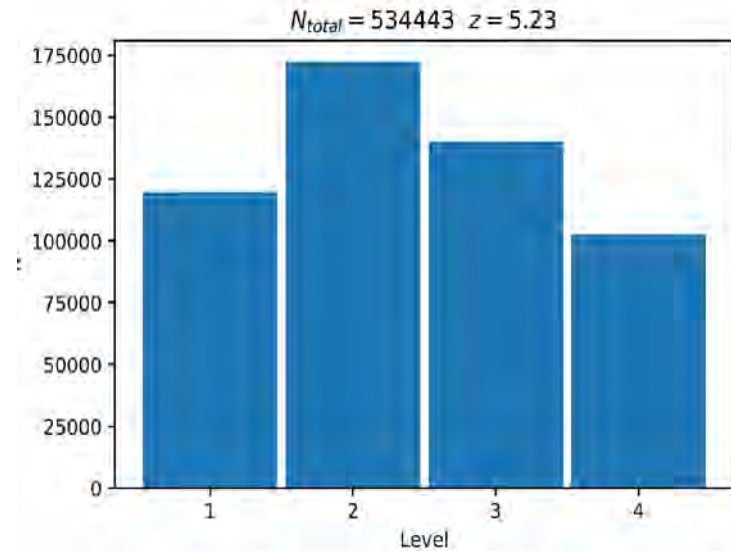
- Precision comparisons between models and simulations require large volumes and high resolution in galaxies
- Standard ENZO code struggles to do this due to limited scalability of its AMR implementation ( $P < 1000$ )
- In 2011, James Bordner and I embarked on a from-scratch redesign and reimplementations of ENZO capable of scaling AMR to millions of cores.
- Blue Waters has been instrumental in the development and testing of ENZO-E

# PRAC: Realistic Simulations of the Intergalactic Medium: The Search for Missing Physics-Part 2



Projection of baryon density in a section of a  $1024^3$ , 25.6 Mpc box with 4 additional levels of refinement. 8K cores, Blue Waters

← ENZO simulation

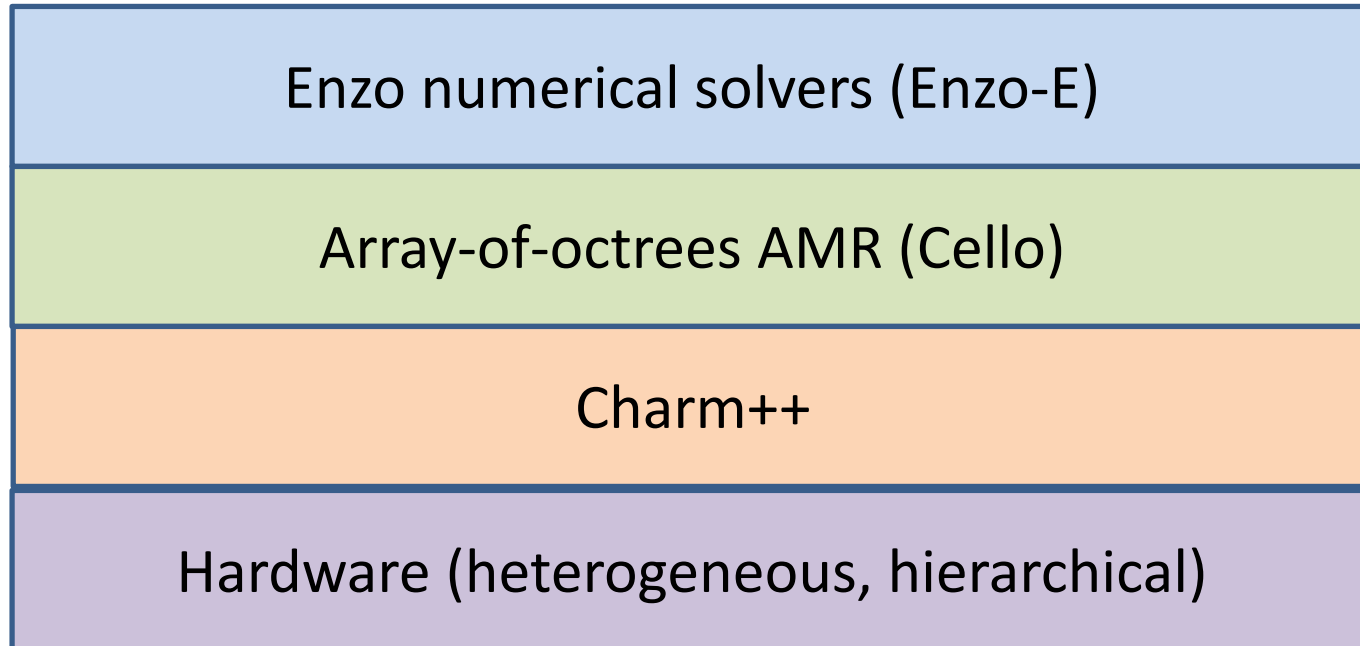


#AMR grids versus level of refinement  
Potential level of concurrency: >100,000

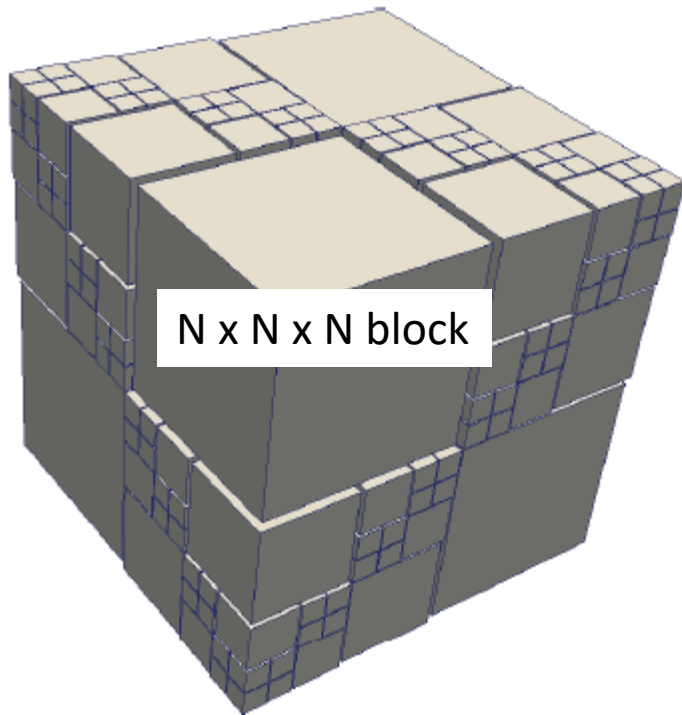
# Adopted Strategy

- Keep the best part of Enzo (numerical solvers) and **replace the AMR infrastructure**
- Implement using modern **OOP best practices** for modularity and extensibility
- Use the best available **scalable AMR algorithm**:
  - **Array-of-Octrees (aka Forest-of-Octrees)**
- Move from bulk synchronous to **data-driven asynchronous execution** model to support patch adaptive timestepping
- Leverage **parallel runtimes** that support this execution model, and have a **path to exascale (Charm++)**
- Make **AMR software library application-independent** so others can use it

# Software Architecture



# How does Cello implement AOT?



2 x 2 x 2 array

- **Array of octrees** of arbitrary size  $K \times L \times M$
- An octree has leaf nodes which are **blocks** ( $N \times N \times N$ )
- Each block is a **chare** (unit of sequential work)
- The entire AOT is stored as a **chare array** using a bit indexing scheme
- Chare arrays are **fully distributed data structures** in Charm++

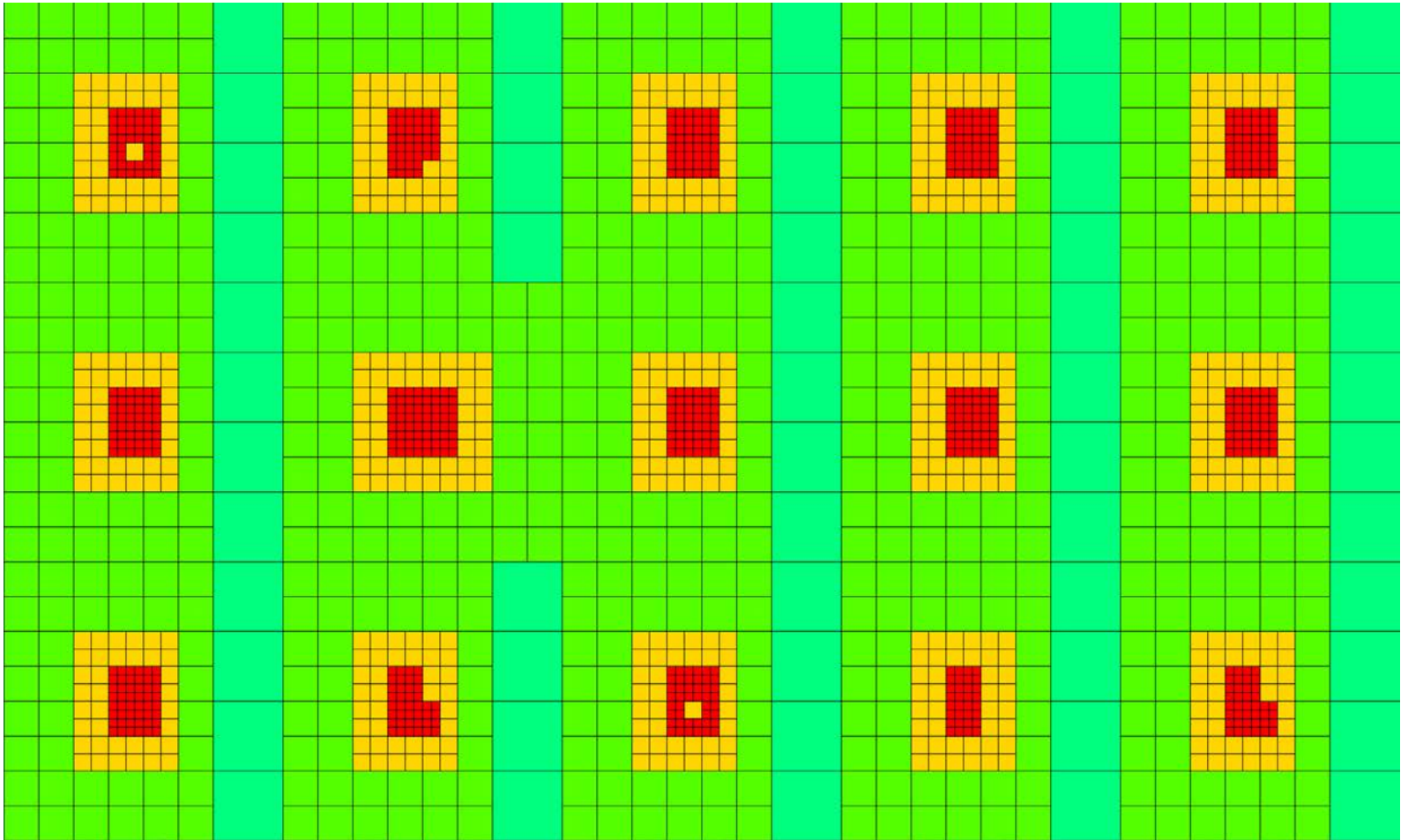
# Demonstration of ENZO-E

Interacting blast waves with PPM solver - Total energy



# Demonstration of ENZO-E

Mesh refinement level;  $32^3$  blocks/chare





# Largest AMR simulation in the world?

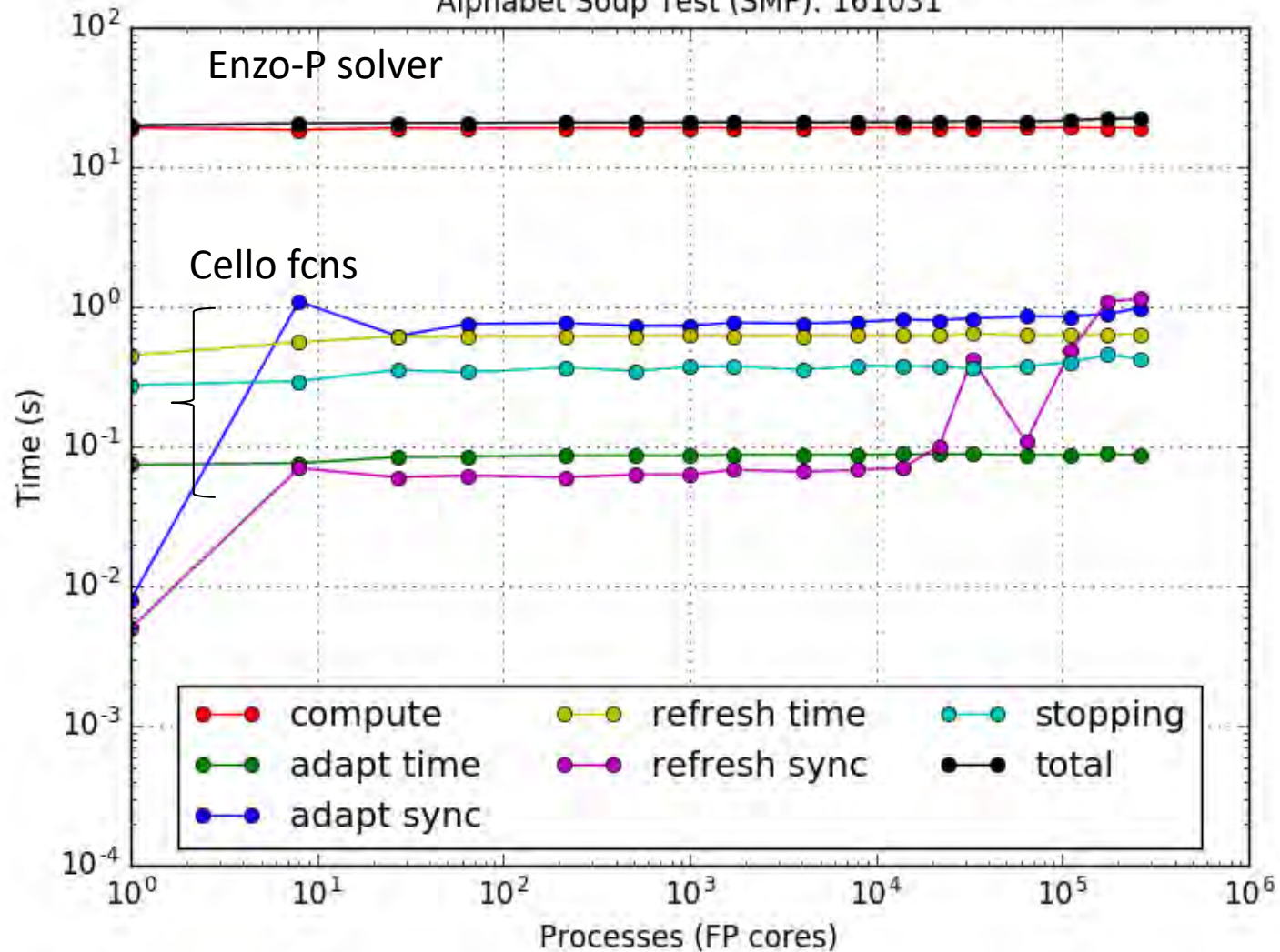
1.7 trillion  
cells

262K cores  
on NCSA  
Blue Waters

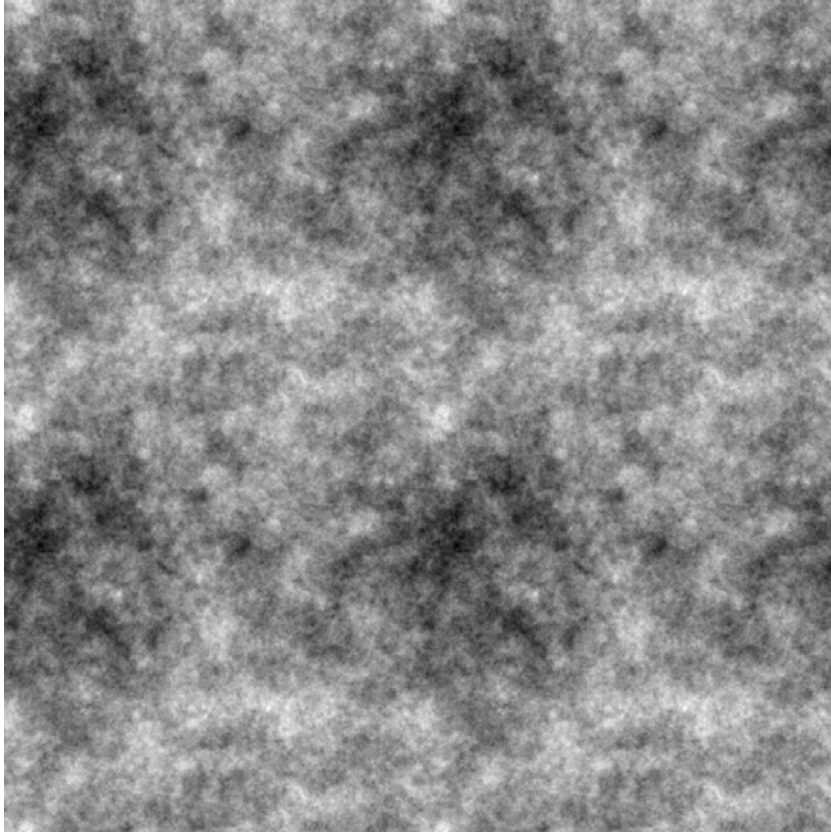
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# Enzo-P Weak Scaling on Blue Waters: Time

Alphabet Soup Test (SMP): 161031



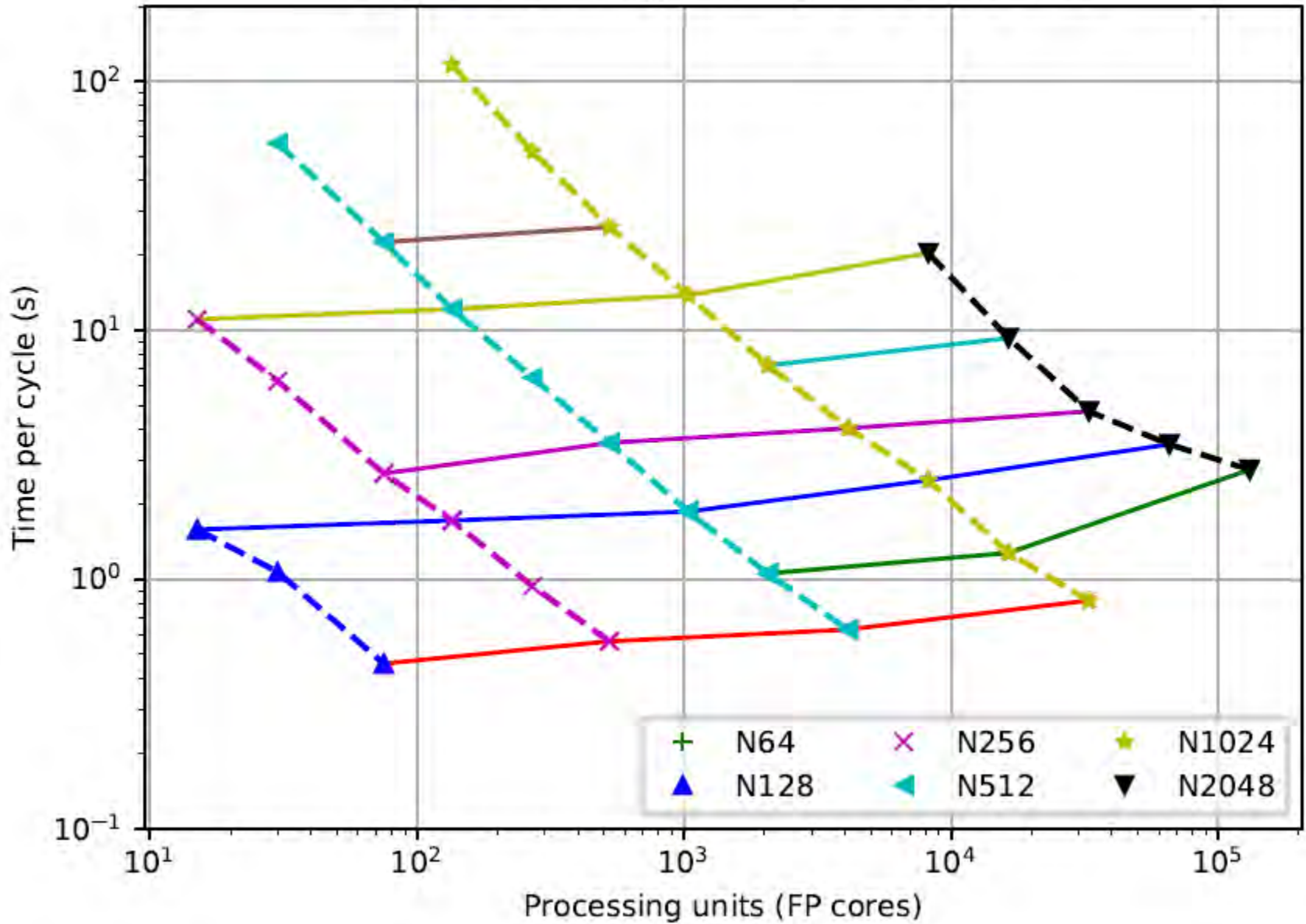
# Hydrodynamic Cosmology Scaling Tests



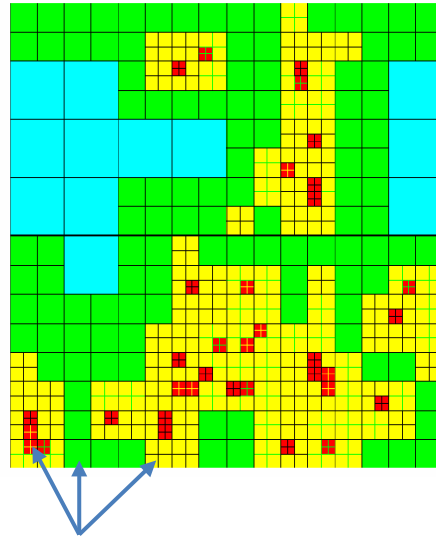
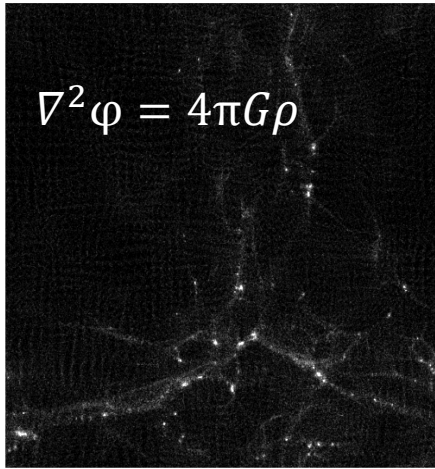
Density projection in  $512^3$  simulation

- Uniform grid only
- Weak and strong scaling
- $32^3$  blocks/chare
- 1, 8, 64 chares/core
- $64^3$  to  $2048^3$  meshes
- $p=8$  to 128k cores

# Enzo-P Cosmology scaling on Blue Waters



# Global Multilevel AMR Poisson Solver

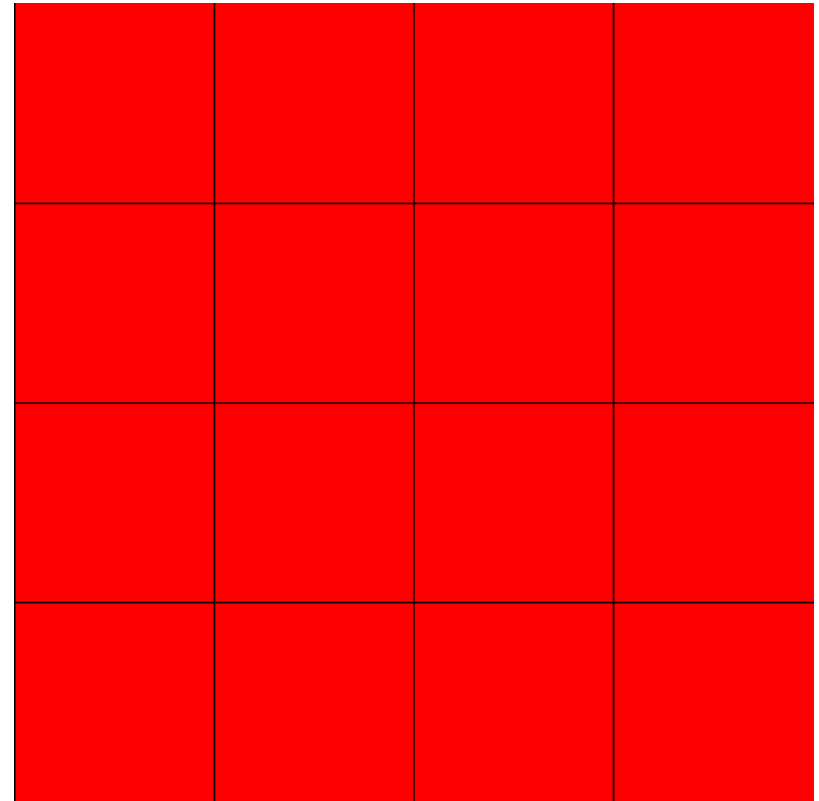
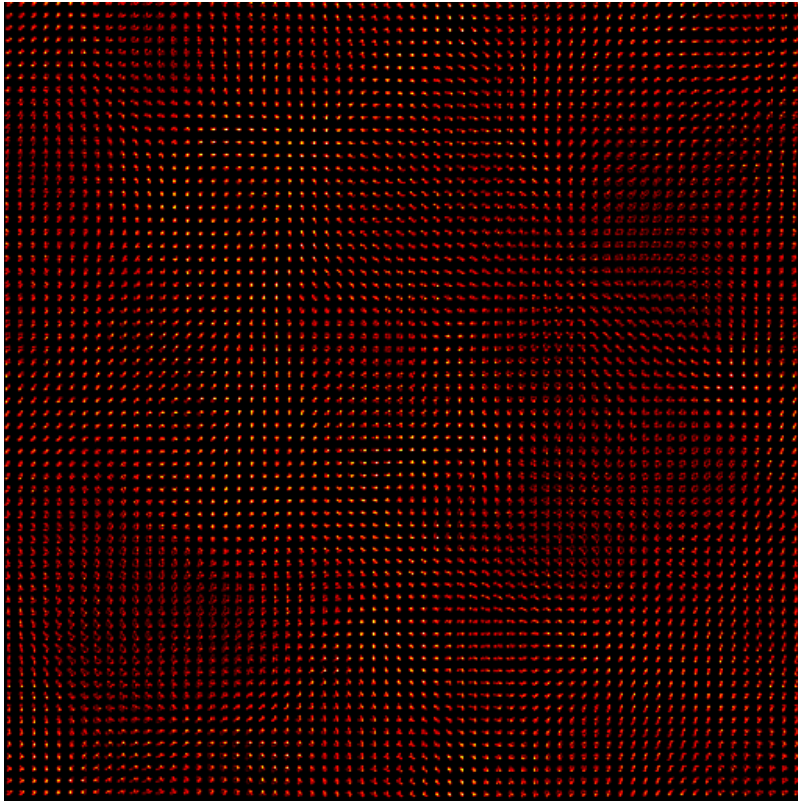


- Each square is projection of  $16^3$  block

- $Ax=b$ 
  - $A$  is non-symmetric matrix arising from discretizing Laplacian operator on multilevel mesh
  - $x$  is gravitational potential  $\phi$
  - $b$  is matter density source term
- Algorithm
  - BiCGStab
    - Diagonally-preconditioned
    - Multigrid-preconditioned
  - Parallelize over all blocks in AOT using Charm++
- poor scalability

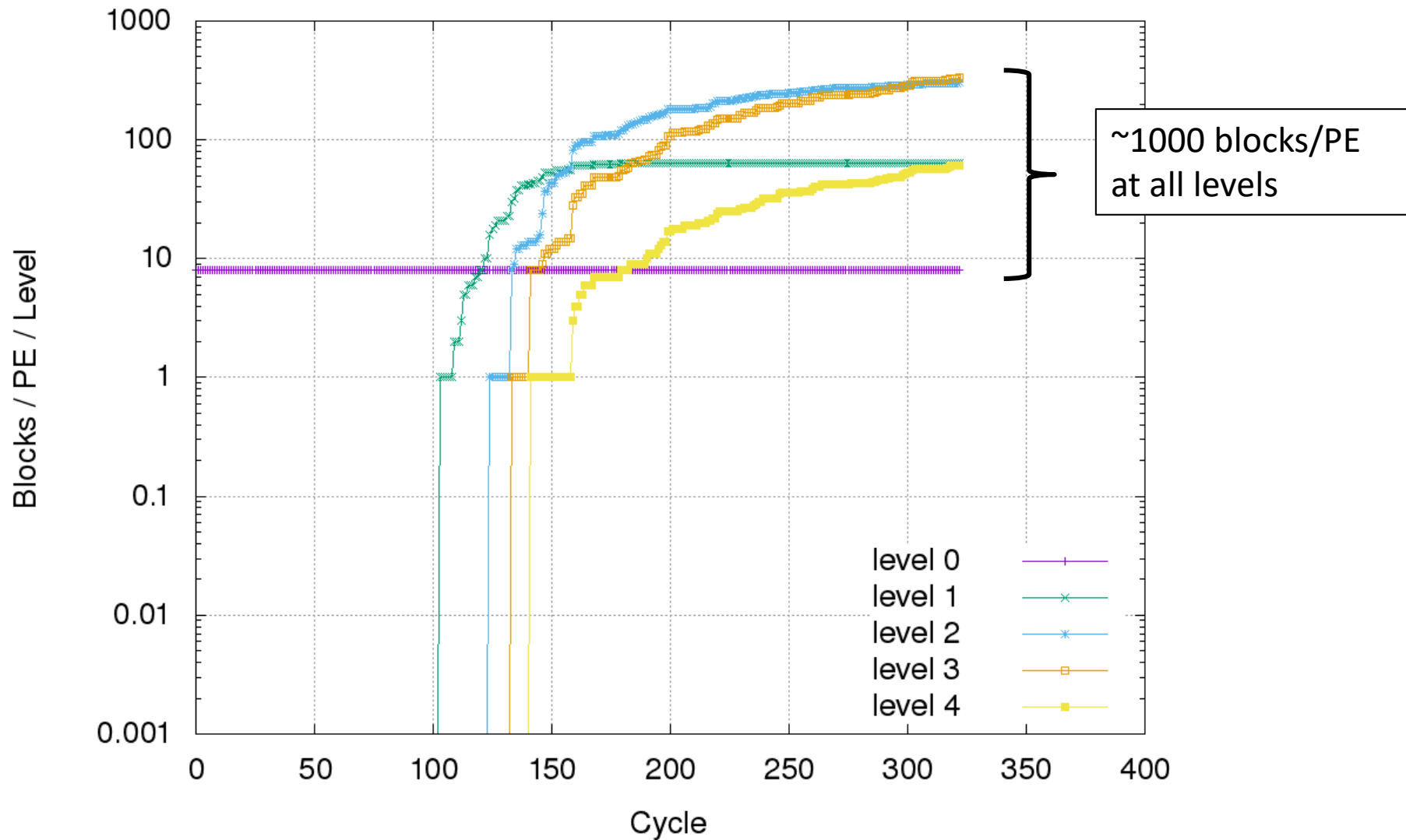
# AMR cosmology with HG\* solver

$64^3$  mesh ( $4^3$  array of  $16^3$  blocks), 4 AMR levels (1024<sup>3</sup> eff.), PE=8

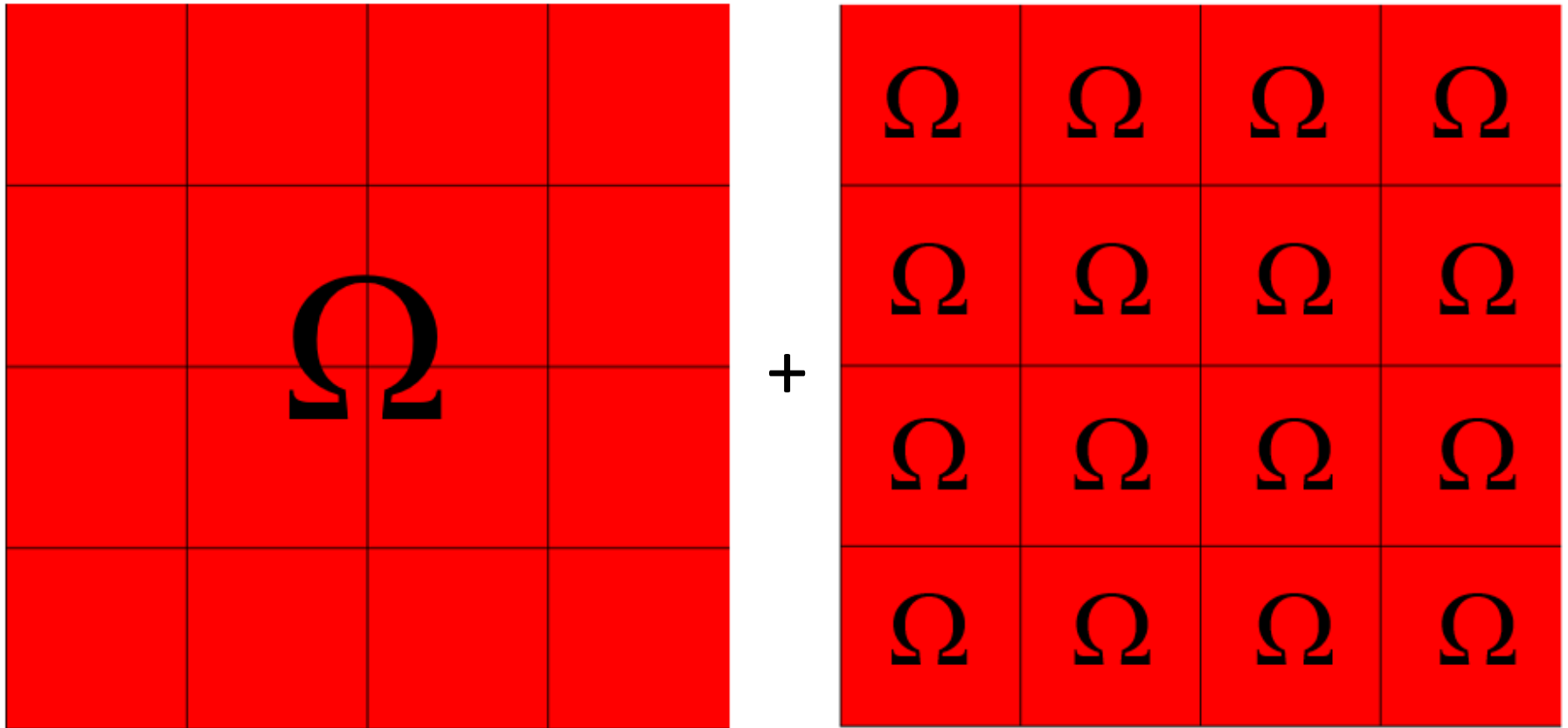


\* HG = multigrid preconditioned BiCGStab

# AMR Cosmology Blocks per Level $N=64^3$ $P=8$



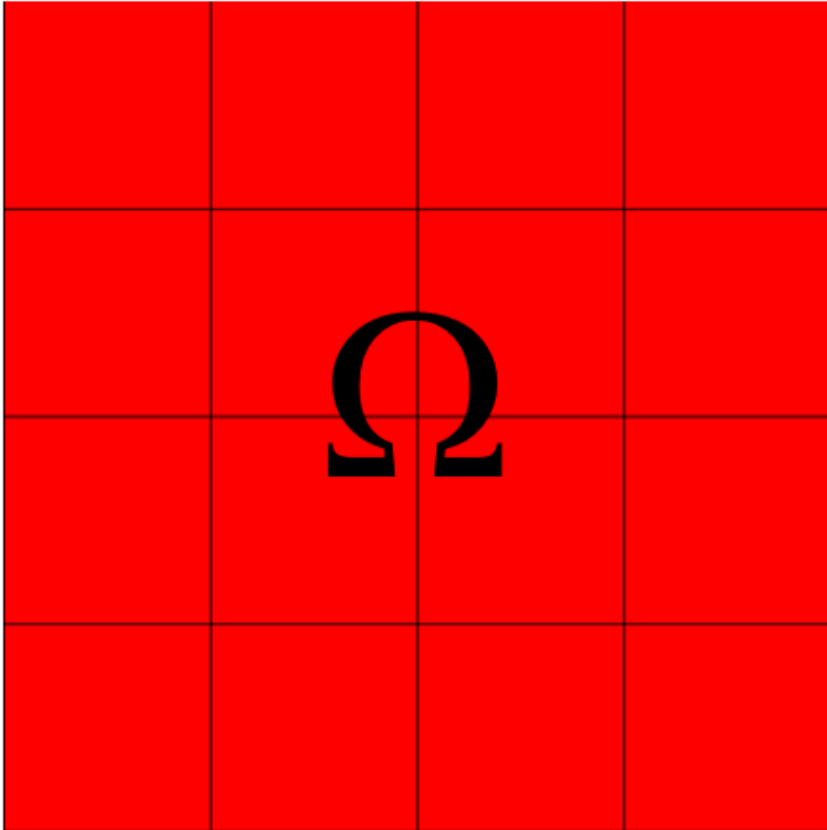
# Domain-decomposed AMR Poisson Solver (DD)



Each block becomes an octree



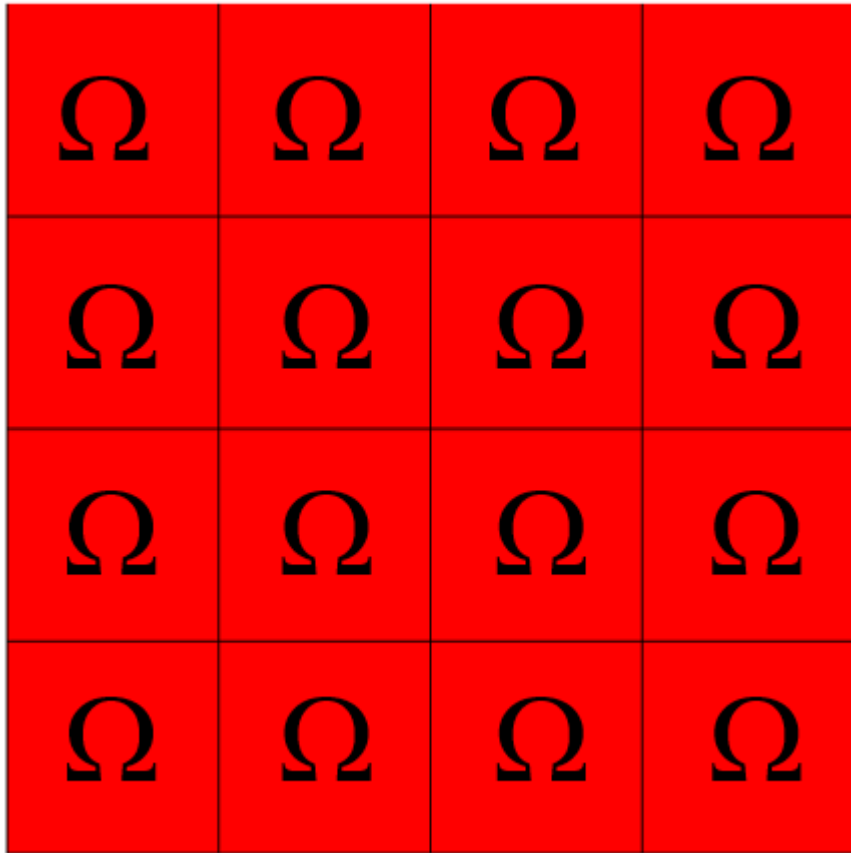
# Domain-decomposed AMR Poisson Solver (DD)



- Step 1: project density field to root grid blocks
- Step 2: global Poisson solve on root grid using multigrid solver
- Step 3: interpolate  $\Phi_0$  to faces of each octree

Each block becomes an octree

# Domain-decomposed AMR Poisson Solver (DD)

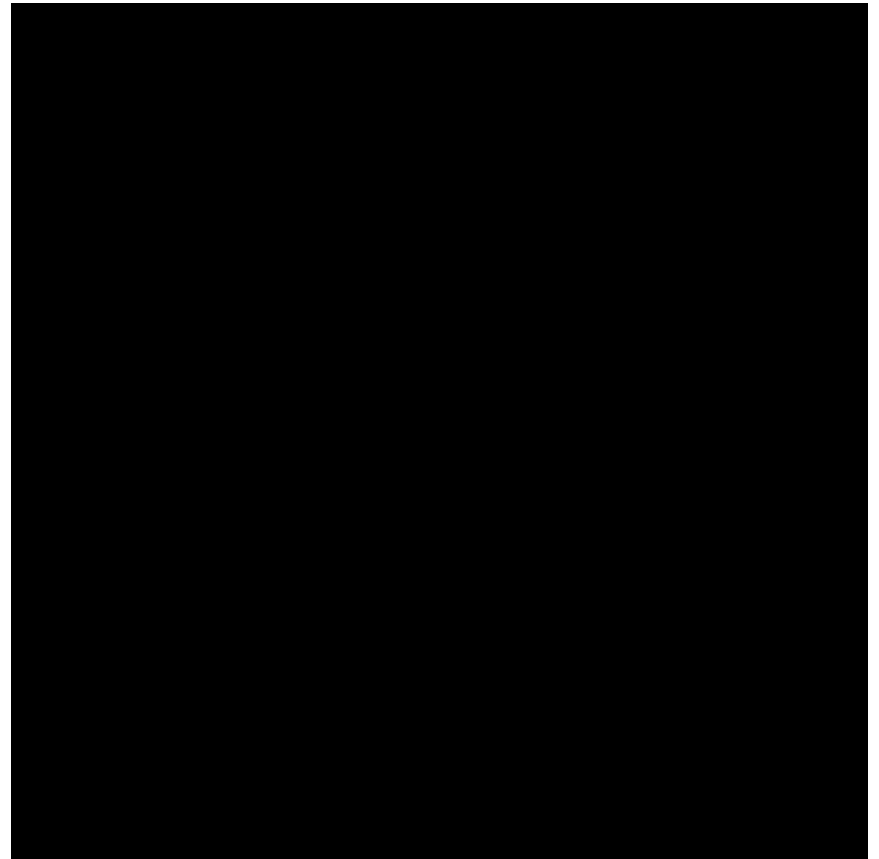
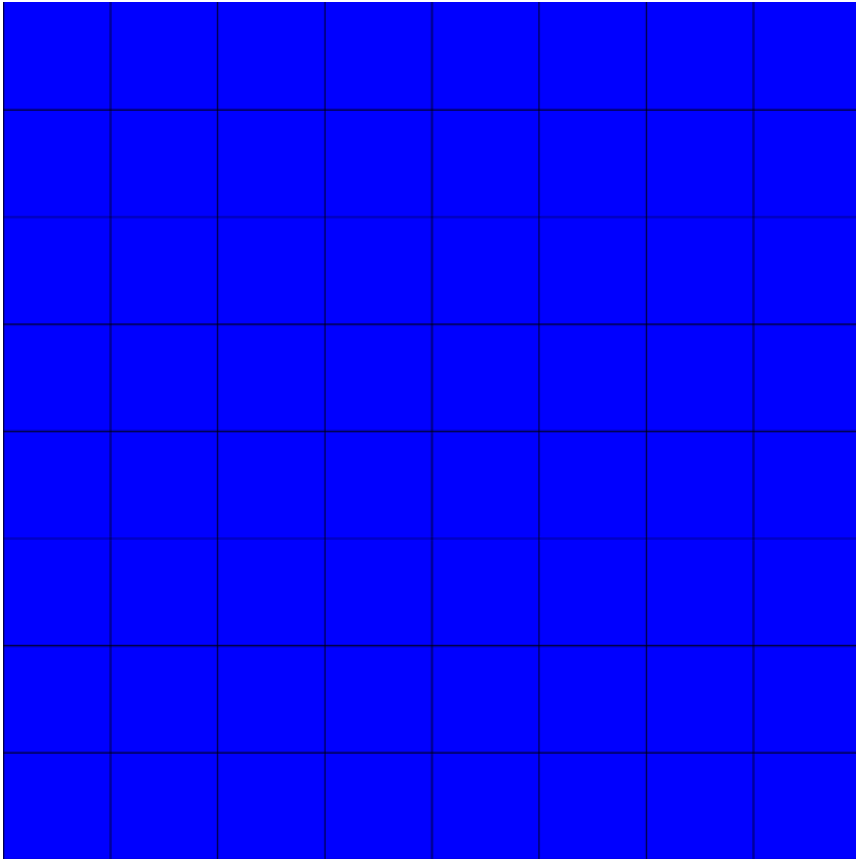


- Step 4: local Poisson solve on each octree using BiCGstab
- Step 5: Jacobi smooth potential  $\Phi_\ell$  on leaf blocks

Each block becomes an octree

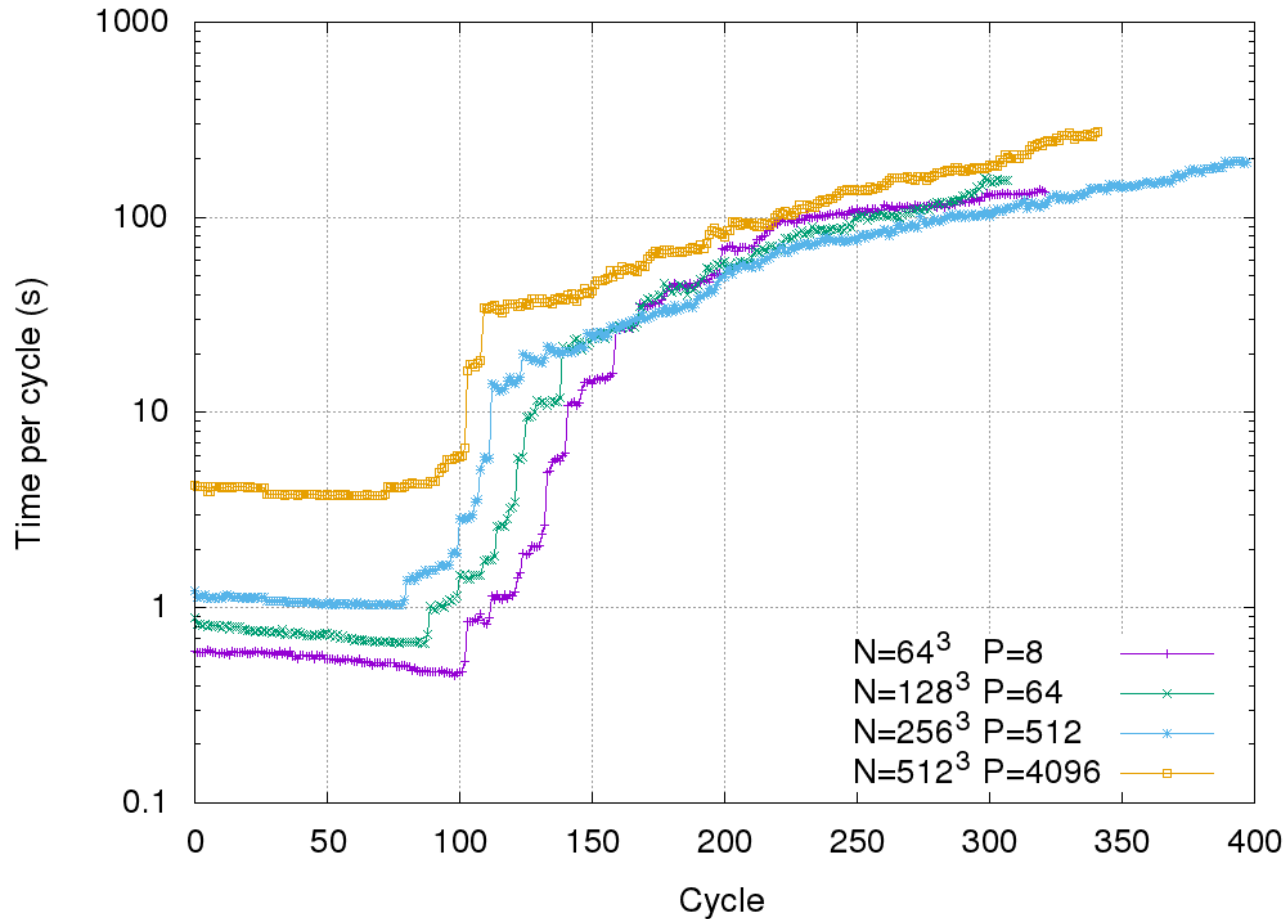
# DD in action

$128^3$  mesh ( $8^3$  array of  $16^3$  blocks), 4 AMR levels ( $2048^3$  eff.), PE=64

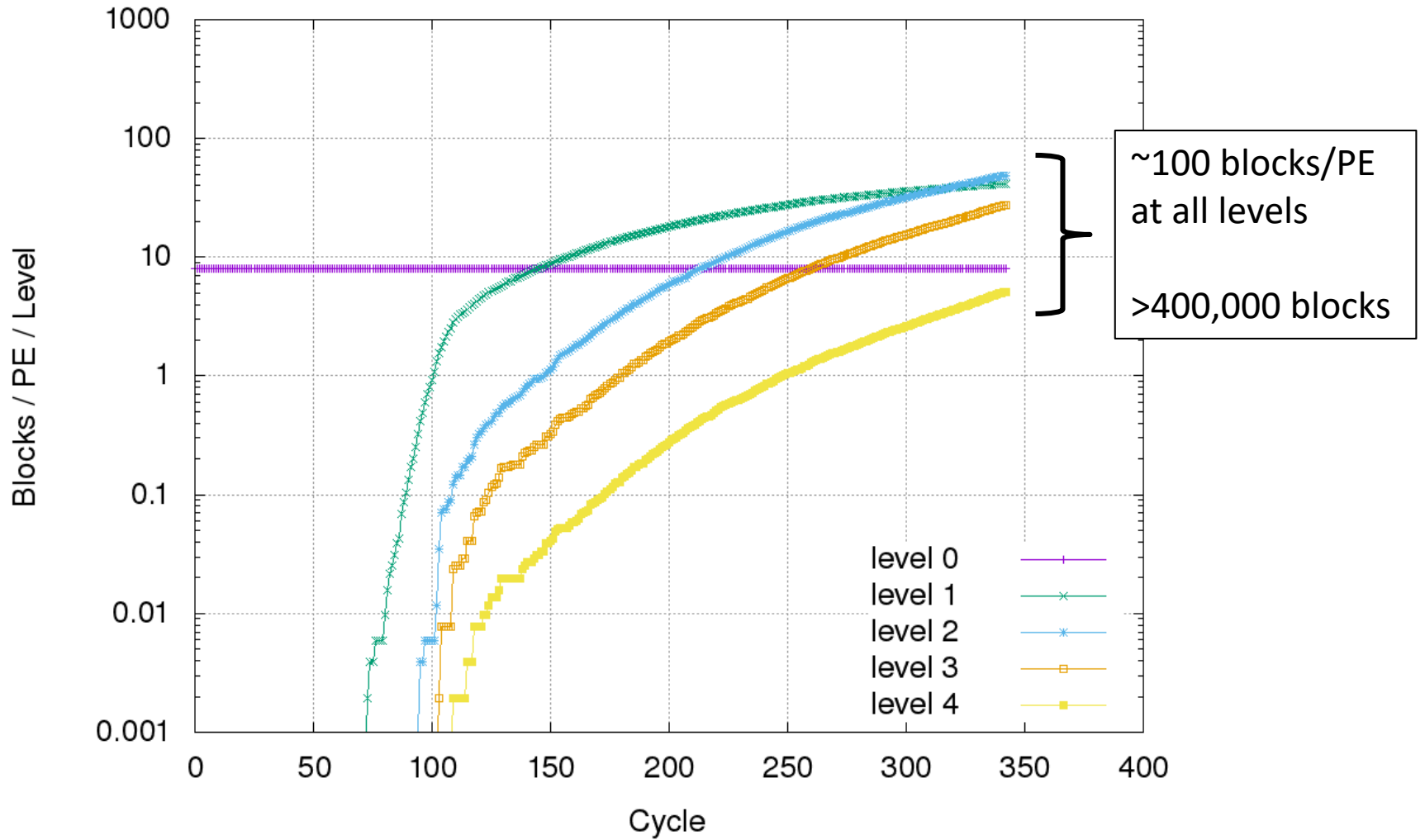


# Is DD scalable? Yes!

AMR Cosmology Weak Scaling on Blue Waters (DD Solver)



# AMR Cosmology Blocks per Level N=512<sup>3</sup> P=4096



# NSF CSSI grant (ENZO-E)

- \$1.9M, 3 years
- Goal: feature-complete implementation of ENZO solvers into ENZO-E
- Goal: migration of ENZO community to ENZO-E
- Goal: implementations for exascale (accelerators)
- PI team
  - Mike Norman, James Bordner (UCSD)
  - Brian O'Shea (MSU)
  - Greg Bryan (Columbia)
  - John Wise (Georgia Tech)

# ENZO-E tasks

- FMM gravity solver
- Block-adaptive local timestepping
- Adaptive ray tracing radiative transfer
- Cosmic ray transport incl. MHD
- Interfacing to GRACKLE chemistry library
- Interface to GPUs using Kokkos
- Lots of scaling/optimization work.....

# Contribution of Blue Waters

- You need a petascale platform to develop an exascale code!
  - Sheer size
  - Balanced architecture
  - Throughput (especially scaling runs)
  - Favorable Q policies
  - Mature SW environment
- Thanks for the memories!!!!